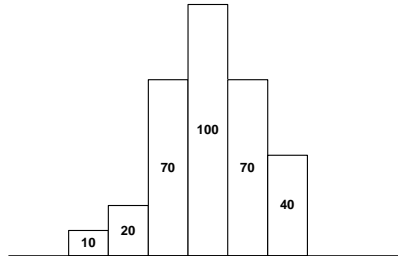


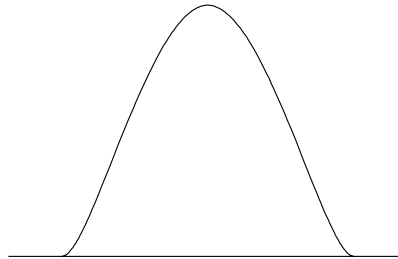
# Essentials of Statistical Process Control

## Sheet 1 - Process Capability

1. Before starting to use statistical process control it is necessary to determine if the process is 'capable' of producing within the specified tolerances. This requires a 'Process Capability Study' to be carried out.
2. Select 50 samples from a continuous run of product.
3. Measure the desired feature and plot results in a histogram using 6 bars.



4. If the distribution is a normal distribution then proceed.



Note: If the distribution is not a normal distribution then other techniques are needed.

Calculate the mean ( $\bar{X}$ ) and the standard deviation ( $\sigma$ ) for the 50 results using a standard calculator.

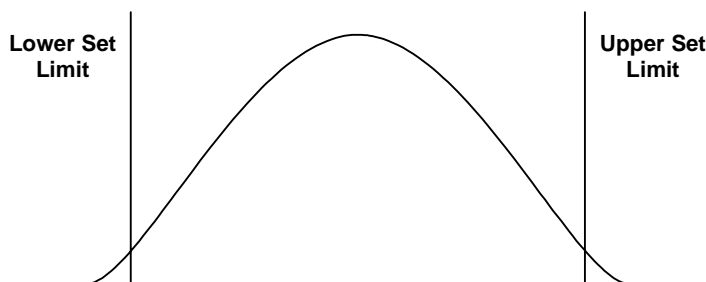
5. Estimate the process variability (relative to the specified tolerances) from the formula:

$$C_p = \frac{USL - LSL}{6\sigma}$$

USL = Upper Set Limit or Upper Acceptable Tolerance.

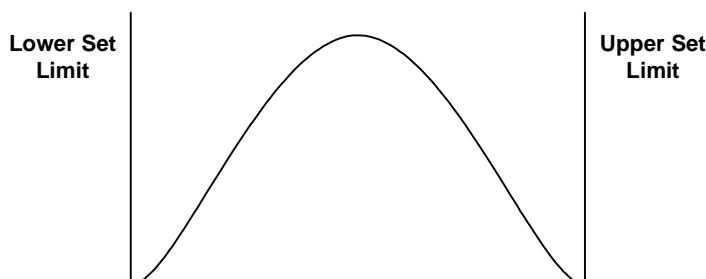
LSL = Lower Set Limit or Lower Acceptable Tolerance.

This value is a measure of the 'process spread'. If  $C_p$  is less than 1.00 then it will not be possible for the process to produce parts within tolerance. When  $C_p$  is  $> 1.33$  the process is said to be 'capable'.



**$C_p$  is less than 1.00**

The process is centred on the tolerances but it will never be possible to produce all the parts inside the tolerance.

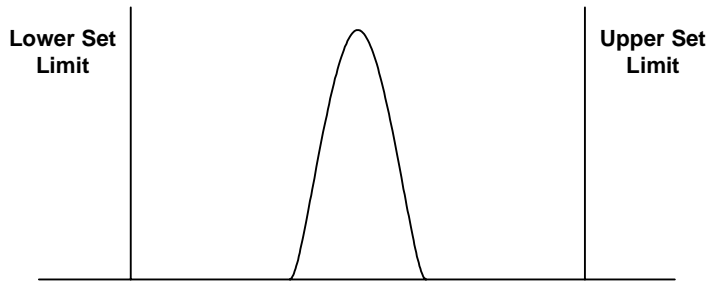


**$C_p$  is equal to 1.00**

It will be possible to produce 99.73% of the parts inside the tolerances but only if the process is exactly centred on the tolerance band and does not vary.

# Essentials of Statistical Process Control

## Sheet 1 - Process Capability



**$C_p$  is greater than 1.33**

The process spread is less than the tolerances. It will be possible to produce all the parts inside the tolerances even with process variations.

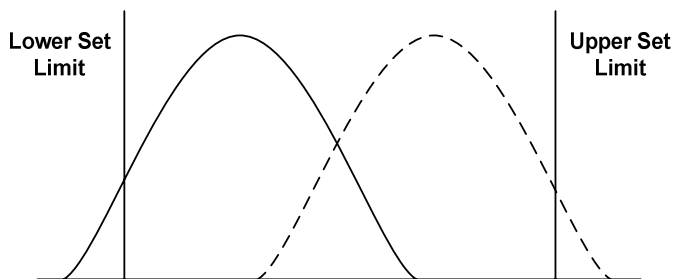
6.  $C_p$  only describes the spread, it does not describe the location and even with a small spread ( $C_p > 1.33$ ) it is possible to produce out of tolerance parts. We need to be able to describe the location of the curve, this is done as follows:

Calculate  $Z_{UPPER}$  and  $Z_{LOWER}$  from the formulae below and find the smaller of the two:

$$Z_{\min} \text{ is the smaller of } Z_{UPPER} = \frac{USL - \bar{X}}{\sigma} \quad \text{and} \quad Z_{LOWER} = \frac{\bar{X} - LSL}{\sigma}.$$

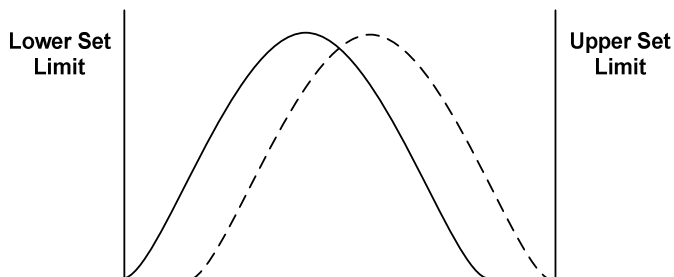
$$C_{pk} = \frac{Z_{\min}}{3},$$

As with  $C_p$ , if  $C_{pk}$  is less than 1.00 then it will not be possible for the process to produce parts within tolerance. When  $C_{pk}$  is  $> 1.33$  the process is said to be 'capable'.



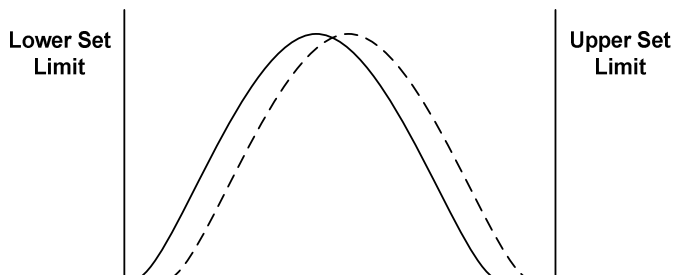
**$C_{pk}$  is less than 1.00**

The process location is outside the tolerances. It will not be possible to produce all the parts inside the tolerances.



**$C_{pk}$  is equal to 1.00**

The process location is inside the tolerances but close to the limits. It will just be possible to produce all the parts inside the tolerances.



**$C_{pk}$  is greater than 1.33**

The process location is well inside the tolerances. It will be easily possible to produce all the parts inside the tolerances.

7. The values for  $Z_{UPPER}$  and  $Z_{LOWER}$  can be used with  $P_z$  tables to calculate the proportion of the output that will be beyond the specification limits.